

# 13\_CSARDL

QuantFit Estimator Standard Operating Procedure

## SOP: Cross-Sectionally Augmented ARDL (CS-ARDL)

Chudik-Pesaran heterogeneous panel ARDL with CSD correction

=> CS-ARDL augments each country's ARDL with cross-sectional means to absorb common factors.

### 1. Purpose

CS-ARDL adds the cross-sectional means of Y and X (and their lags) to each country's ARDL specification. This proxies for unobserved common factors driving cross-sectional dependence, restoring consistent estimation of the long-run coefficients.

### 2. When to use this estimator

Panel ARDL with confirmed CSD (Pesaran CD  $p < 0.05$ ).

Slope heterogeneity present.

Large N and moderate T.

### 3. Required data structure

Balanced panel preferred.

Same I(0)/I(1) conditions as ARDL.

### 4. Mathematical formulation

Per-country UECM augmented with cross-sectional means:

$$\Delta Y_{i,t} = \alpha_i + \phi_i (Y_{i,t-1} - \lambda_i' X_{i,t-1}) + \text{Sum ?} \\ \Delta X + \text{Sum } \mu Z_{t-l} + \epsilon_{i,t}$$

$Z_{t-l}$  = cross-sectional means of (Y, X) at lag l

Per-country estimation; long-run = cross-country average.

### 5. Pre-estimation diagnostics

Pesaran CD => rejection motivates CS-ARDL.

Slope homogeneity test.

Per-country ARDL pre-checks.

### 6. Estimation procedure

Compute cross-sectional means of Y and X at each t.

Per-country ARDL with cross-sectional means and lags appended.

Cross-country average of  $\lambda_i$ .

Floor  $pT = \text{floor}(T^{1/3})$  lags of cross-section means.

## 7. Output produced

## 8. Output interpretation

Long-run estimate consistent under CSD plus heterogeneity.

CS-mean coefficients absorb the influence of unobserved common factors.

## 9. Post-estimation diagnostics

Pesaran CD on residuals (should be eliminated).

Slope homogeneity ex-post.

## 10. Common pitfalls

Adding too many lags of cross-section means depletes degrees of freedom.

Strong CSD with small N can leave residual CSD.

## 11. Reporting checklist

Pesaran CD before and after CS augmentation.

Per-country selected lag orders.

Long-run table with cross-sectional SE.

Cross-section mean coefficient table.

## 12. References

Chudik, A., Pesaran, M. H. (2015). Common correlated effects estimation of heterogeneous dynamic panel data models with weakly exogenous regressors.

Field | Meaning

longRunCoefficients | Average per-country lambda?

longRunSE | Cross-sectional SE

csMeanCoefficients | Cross-sectional mean coefficients (mu?)

unitResults | Per-country fit including CS columns

ect | Average per-country phi?